In the “traditional” processor we run one thread and issue instructions from this to the multiple pipelines.
Problems with “traditional” processor design:

#1: Running out of ILP
Not enough instructions to feed pipelines

#2: Wire delay is starting to hurt
Thinner wires, higher resistance, slower speed

#3: Memory is the bottleneck
Slow memory accesses stalls the execution

#4: Power is the limit, $P \sim F^2 V^2$
Cooling problem, high energy cost, low battery time

Solving all the problems, exploring parallelism:

#1: Running out of ILP
> Feed one CPU with instructions from many threads

#2: Wire delay is starting to hurt
> Multiple small cores with private L1$, shorter paths

#3: Memory is the bottleneck
> Overlap memory accesses from many threads

#4: Power is the limit
> Multiple cores, lower F and V, better performance
SMT: Simultaneous MultiThreading

Can feed the multiple pipelines with instruction from many threads.

Overlap memory accesses with computations
CMP: Chip MultiProcessor (MultiCore)

Thread 1

Thread N

Example: Intel Core i7

QuickPath Interconnect

3x DDR-3 DRAM

L3 8MB

X-bar

L2$ 256kB L2$ 256kB L2$ 256kB L2$ 256kB

CPU, 2 thr. CPU, 2 thr. CPU, 2 thr. CPU, 2 thr.
Multi-Processor, Multi-Core PCs with powerful GPU cards are here! Number of cores are increasing in each generation, our computers are becoming more and more parallel!

⇒ Need parallel programming on all levels and applications (OS, Games, Internet servers, Data bases, Scientific applications, etc). Impossible to do automatically, compilers can not analyze all dependencies.

To exploit the full potential of our computers we need to explicitly parallelize our codes!
**Throughput computing:**
(Run P instances of the same program in parallel)

- Interfere in cache utilization (bad performance)
- Requires P times more memory
- Problems get worse with increased P

If limited by mem capacity/bandwidth go parallel

Example: "Lattice Boltzmann Method" to simulate incompressible fluids in 3D on a quad-core processor

---

**What is Parallel Computing**

Traditionally, software has been written for *serial* computation:

- To be run on a single computer having a single CPU.
- A problem is broken into a discrete series of instructions.
- Instructions are executed one after another.
- Only one instruction may execute at any moment in time.
In the simplest sense, parallel computing is the simultaneous use of multiple compute resources to solve a computational problem:

- A problem is broken into discrete parts that can be solved concurrently
- Each part is further broken down to a series of instructions

**Parallel Programming models**

Two main models (scientific computing)

1. Local name space or private memory
   - C/C++/(Fortran) and **MPI**
2. Global name space or shared memory
   - C/C++/(Fortran) and **OpenMP/Pthreads**

**SPMD** - Single Program Multiple Data
(All processors run the same program)

Parallelism through data ownership and/or branches (if MyPid==1 then)
Need to communicate and synchronize!
Working with MPI we have a local address space model. The processes cannot access and change variables residing on remote memory. A variable \( x \) can have different values on different processes. All variables are *private* to the processes.

To share data we need to explicitly communicate data between processes. For this we use the MPI library, *Message Passing Interface*.
MPI: Message Passing Interface (1994)

Used on PC-Clusters and other large parallel computers. Each process has its own private address space => Data is shared through explicit communication calls (library).

Point-to-point: MPI_Send - MPI_Recv
Collective calls: MPI_Bcast, MPI_Reduce, etc
[Over 430 MPI function]

Need to specify exactly how to divide data and what each processor should do and who to communicate with => low-level model
But a scalable model with high performance!

Global name space model

Working with Pthreads and OpenMP we have a global shared space model. Each thread can access and change the global variables.
**Pthreads:** POSIX threads (1995)

Used on multi-core machines and other shared memory computers. Shared address space model, based on threads (“light weight process”). All threads have access to global data.

Memory coherence handled by hardware but requires explicit synchronization and protection of shared variables from multiple updates.

Low-level model but easier to program as data is global to all threads (no need to explicitly create ownership and communicate data between processors). Still need to divide work manually and synchronize threads.

**OpenMP:** Open spec for Multi Processing (1997)

Used on multi-core machines and other shared memory computers. Shared address space model, based on threads. All threads have access to global data. Memory coherence handled implicitly by compiler (and hardware).

Insert compiler directives for parallelization of computations => high-level model

```
#pragma omp parallel for
for (i=1;i<N-1;i++)
```

Loop is automatically parallelized over all threads, arrays A and B are global data.
What is a thread?

“Technically, a thread is defined as an independent stream of instructions that can be scheduled to run as such by the operating system.”

- Exists within a process and uses the process resources
- Has its own independent flow of control as long as its parent process exists and the OS supports it
- Duplicates only the essential resources it needs to be independently schedulable, e.g., program counter
- May share the process resources with other threads that act equally independently, e.g., shared memory
- Dies if the parent process dies - or something similar
- Is "lightweight" because most of the overhead has already been accomplished through the creation of its process.

A thread is a “lightweight process”, it contains it own:

- Program counter
- Registers and stack pointer
- Scheduling properties (such as policy or priority)
- Set of pending and blocked signals

Compare with a Unix process:

- Process ID, process group ID, user ID, and group ID
- Environment
- Working directory
- Program instructions
- Registers, Stack, Heap
- File descriptors
- Signal actions
- Shared libraries
- Inter-process communication tools

\[
\begin{align*}
\text{fork()} & \quad \text{fork}() \\
\text{pthread_create()} & \quad \text{thread}() \\
\end{align*}
\]

10:1
Two threads in a process space

Multiple threads sharing process resources =>

- Changes made by one thread to shared system resources (such as closing a file) will be seen by all other threads.
- Two pointers having the same value point to the same data.
- Reading and writing to the same memory locations is possible, and therefore requires explicit synchronization by the programmer.
Traditionally threads have been used to:

- Overlapping CPU work with I/O: For example, a program may have sections where it is performing a long I/O operation. While one thread is waiting for an I/O system call to complete, CPU intensive work can be performed by other threads.

- Priority/real-time scheduling: tasks which are more important can be scheduled to supersede or interrupt lower priority tasks.

- Asynchronous event handling: tasks which service events of indeterminate frequency and duration can be interleaved. For example, a web server can both transfer data from previous requests and manage the arrival of new requests.

On Multi-Core processors we can use the parallel cores to run several processes/applications in parallel or we can parallelize on application using threads and schedule the threads to different cores.
Common parallelization strategies:

- **Manager/worker:** a single thread, the manager assigns work to other threads, the workers. Typically used when we have a dynamic pool of *tasks with irregular work load*.

- **Peer:** similar to the manager/worker model, but after the main thread creates other threads, it participates in the work. Typically used for *static homogeneous tasks*.

- **Pipeline:** a task is broken into a series of sub operations, each of which is handled in series, but concurrently, by a different thread. An automobile *assembly line* best describes this model. Used for large dependent tasks.

**POSIX threads or pthreads**

*Portable Operating System Interface for UNIX*

Portable standard for thread programming, specified by the IEEE POSIX 1003.1c standard (1995). C Language only!

The Pthreads API contains over 60 subroutines which can be grouped into three major classes:

- **Thread management:** creating, terminating, joining
- **Mutexes:** provides exclusive access to code segments and variables with the use of locks (mutual exclusion)
- **Condition variables:** provides synchronization and communication between threads that share a mutex
Creating and terminating threads:

**Pthread_create( threadptr, threadattr, func, funcarg )**

Creates a thread which starts running the specified function. Once created, threads are peers, and may create other threads. There is no implied hierarchy or dependency between threads.

There are several ways in which a Pthread may be terminated:

- The thread returns from its starting routine
- The thread makes a call to `pthread_exit()`
- The thread is canceled by another thread via the `pthread_cancel()` routine
- The entire process is terminated, i.e., main() finishes without self calling `pthread_exit()`

**Note:** By calling `pthread_exit()` also in main(), i.e., on the master thread, all threads are kept alive even though all of the code in main() has been executed. Can also do explicit wait with `pthread_join()`
Example HelloWorld:

```c
#include <pthread.h>
#include <stdio.h>
#define NUM_THREADS     5

void *HelloWorld(void *arg){
    printf("Hello World!\n");
    pthread_exit(NULL);
}

int main (int argc, char *argv[]){
    pthread_t threads[NUM_THREADS];
    int t;
    for(t=0; t<NUM_THREADS; t++)
        pthread_create(&threads[t], NULL,
                        HelloWorld, NULL);
    pthread_exit(NULL);
}
```

Task: Compile and run the program helloworld.c

- gcc -pthread helloworld.c -o hello
- Run on different number of threads. Without re-compiling?
- How can we implement a threadID in the thread function?
- Why do we need pthread_exit() in main?

Example HelloWorld:

```c
#include <pthread.h>
#include <stdio.h>
#define NUM_THREADS     5

void *HelloWorld(void *arg){
    long thid=(long)arg;
    printf("Hello World %ld!\n", thid);
    pthread_exit(NULL);
}

int main (int argc, char *argv[]){
    pthread_t threads[NUM_THREADS];
    long t;
    for(t=0; t<NUM_THREADS; t++)
        pthread_create(&threads[t], NULL,
                        HelloWorld, (void *)t);
    pthread_exit(NULL);
}
```

Passing arguments:

Note, can only pass one argument of type void*

- How can we pass several arguments and other types?
Passing arguments:
Use structs and type cast the address of the struct to void*

```
struct thread_data{
   int field1;
   double field2;}

void *HelloWorld(void *arg){
   struct thread_data *my_data = (struct thread_data*) arg;
   int f1 = my_data -> field1;
   double f2 = mydata -> field2;
   _ }

int main (int argc, char *argv[]){
   struct thread_data data;
   data.field1=5; data.field2=3.14;
   pthread_create(&threads[t], NULL, HelloWorld, (void*)&data);
   _ }
```

Task: Study, compile and run the program hello_arg2.c
Modify the program to pass different messages to the different threads (different greetings). Note the return value!

Joining threads (waiting):

\textit{Pthread join( threadptr, status )}
Blocks the calling thread until the specified thread terminates.

When a thread is created, its attribute must define joinable
To explicitly create a thread as joinable:

- Declare a pthread attribute variable of the pthread_attr_t data type

- Initialize the attribute variable with pthread_attr_init()

- Set the attribute detached status with pthread_attr_setdetachstate()

- When done, free library resources used by the attribute with pthread_attr_destroy()

Joinable threads (wait to complete):

```c
pthread_attr_t attr;
pthread_attr_init(&attr);
pthread_attr_setdetachstate(&attr, PTHREAD_CREATE_JOINABLE);
for (t=0; t<NUM_THREADS; t++)
    pthread_create(&thread[t],&attr,func,(void *)&data);
pthread_attr_destroy(&attr);
for (t=0; t<NUM_THREADS; t++)
    pthread_join(thread[t], &status);
```

Can also set the state to PTHREAD_CREATE_DETACHED
(Default value is joinable.)

Other attributes that can be set are stacksize and scheduling policy. (For more info see Pthreads manual.)
Example join:
Joining threads is useful when we have several parallel sections, then join threads between and spawn new threads for each parallel function. Or if we want to compute something on the master in the end that depends on the result of the threads.

Task: Study, compile and run the program join.c
Note how the status variable is used.
Is join motivated in this case, what happens if we remove it?

Global and local data:
Data allocated on the stack, i.e., within functions, is local and private to the threads. All other data is global.

```c
// Global data accessible to all threads
int GlobData[Nsize];

void *threadfunc(void *arg){
  // Local data private to the calling thread
  int LocData[Nsize];
  ...
}

int main(int argc, char *argv){
  // Private to master but can be passed to threads
  // as a globally shared array using its address
  int MasterData[Nsize];
  ...
}
```
Global and local data:

Task: What variables are local (private) and what variables are global (shared) in the program data.c?

Is the output what you expected? Are there any suspicious operations in the code? Run the code several times to see if the output changes.

Explain what happens.

Mutex (mutual exclusion) variables:

Mutex variables are one of the primary means of implementing thread synchronization and for protecting shared data when multiple writes occur.

<table>
<thead>
<tr>
<th>Thread 1</th>
<th>Thread 2</th>
<th>Balance</th>
</tr>
</thead>
<tbody>
<tr>
<td>Withdraw: 1500</td>
<td>Deposit: 1000</td>
<td>500</td>
</tr>
<tr>
<td>Read: 3000??</td>
<td>Read: 3000!!</td>
<td>3000</td>
</tr>
</tbody>
</table>

Example without protection of the shared Balance
A typical sequence in the use of a mutex is as follows:

- Create and initialize a mutex variable
- Several threads attempt to lock the mutex
- Only one succeeds and that thread owns the mutex
- The owner thread performs some set of actions
- The owner unlocks the mutex
- Another thread acquires the mutex and repeats the process
- Finally the mutex is destroyed

When several threads compete for a mutex, the losers block at that call - an unblocking call is available with "trylock" instead of the "lock" call. (Trylock is much faster, it does not block but it also does not have to deal with queues of multiple threads waiting on the lock.)

Mutex functions:

```c
pthread_mutex_init( mutex, attr )
pthread_mutex_lock( mutex )
pthread_mutex_trylock( mutex )
pthread_mutex_unlock( mutex )
pthread_mutex_destroy( mutex )
```

The mutex attribute can be set to:

- PTHREAD_MUTEX_NORMAL_NP
- PTHREAD_MUTEX_RECURSIVE_NP
- PTHREAD_MUTEX_ERRORCHECK_NP

Or just use attr=NULL for default values.
Example Mutex

```c
#include <pthread.h>
#define NUM_THREADS 5
pthread_mutex_t mutexsum;
int sum=0;

void *addone(void *arg)
{  
    pthread_mutex_lock (&mutexsum);
    sum += 1;
    pthread_mutex_unlock (&mutexsum);
    pthread_exit(NULL);
}

int main (int argc, char *argv[])
{  
    pthread_mutex_init (&mutexsum, NULL);
    for(t=0; t<NUM_THREADS; t++)
        pthread_create(&threads[t], NULL, addone, NULL);
    ...
}
```

**Task:** Modify the program sum.c such that each thread adds its local sum to the global sum instead of master.

Condition variables:

A condition variable is used for synchronization of threads. It allows a thread to block (sleep) until a specified condition is reached.

- `Pthread_cond_init( cond, attr )` - use attr=NULL
- `Pthread_cond_wait( cond, mutex )` - block thread
- `Pthread_cond_signal( cond )` - wake one thread
- `Pthread_cond_broadcast( cond )` - wake all threads
- `Pthread_cond_destroy( cond )`

A condition variable is always used in conjunction with a mutex lock. Proper locking and unlocking of the associated mutex variable is important.
Pthread_cond_wait():

```c
pthread_mutex_lock(mutexvar);
if (status!="final")
    pthread_cond_wait(condvar,mutexvar);
pthread_mutex_unlock(mutexvar);
```

Pthread_cond_wait blocks a thread until the condition variable is signaled. It will automatically release the mutex while it waits. After the thread is awakened, mutex will be automatically locked for use by the thread. Note, wait does not use any CPU cycles until it is woken up (mutex_lock uses CPU cycles for polling).

Pthread_cond_signal(), pthread_cond_broadcast():

```c
pthread_mutex_lock(mutexvar);
if (status=="final")
    pthread_cond_signal(condvar);
pthread_mutex_unlock(mutexvar);
```

The pthread_cond_signal() routine is used to wake up another thread which is waiting on the condition variable. It should be called after mutex is locked, and must unlock mutex in order for pthread_cond_wait() routine to complete.

If more than one thread is in a blocking wait can then use pthread_cond_broadcast() to wake all.
Example: barrier

```c
#include <pthread.h>

void barrier()
{
    int mystate;
    pthread_mutex_lock (&lock);
    mystate = state;
    waiting++; // Increment waiting counter
    if (waiting == nthreads) {
        waiting = 0;
        state = 1 - mystate;
        pthread_cond_broadcast (&signal);
    }
    while (mystate == state) {
        pthread_cond_wait (&signal, &lock);
    }
    pthread_mutex_unlock (&lock);
}
```

**Note 1:** Use while-statement as spurious wake ups of threads sleeping in wait may occur.

**Note 2:** In some implementations there is a barrier
```
#include <pthread.h>

pthread_barrier_t barr;

void barrier()
{
    pthread_barrier_init (&barr, NULL, nthreads);
    pthread_barrier_wait (&barr);
}
```

**Note 3:** It is possible to design your own special barrier

Example: spinwait

A simpler way to implement a barrier would be to constantly read a global variable until it changes.

```c
#include <pthread.h>

void barrier()
{
    int mystate;
    pthread_mutex_lock (&lock);
    mystate = state;
    waiting++; // Increment waiting counter
    if (waiting == nthreads) {
        waiting = 0;
        state = 1 - mystate;
    }
    while (mystate == state) {
        pthread_mutex_unlock (&lock);
        while (mystate == state);
    }
}
```

**Task:** This is implemented in the code spinwait.c, run the code. What is the problem with this barrier and how can it be fixed? What are the pros and cons with respective barrier?
Case Studies

Example: Enumeration sort

```c
for (j=0;j<len;j++)
{
    rank=0;
    for (i=0;i<len;i++)
        if (indata[i]<indata[j]) rank++;
    outdata[rank]=indata[j];
}
```

Where is the parallelism? Identify parallel tasks!

Solution: `enumsort.c` Manager-Worker

For each task (element) start a new thread, but start only a set of concurrent threads at a time.

```c
for (j=0;j<len;j+=NUM_THREADS){    /* Manager */
    for(t=0; t<NUM_THREADS; t++){
        el=j+t;
        pthread_create(&threads[t],&attr,findrank,(void*)el);}
    for(t=0; t<NUM_THREADS; t++)
        pthread_join(threads[t], &status);
}

void *findrank(void *arg){    /* Worker */
    int rank=0,i;long j=(long)arg;
    for (i=0;i<len;i++)
        if (indata[i]<indata[j]) rank++;
    outdata[rank]=indata[j];
    pthread_exit(NULL);}
```
Task: Study, compile and run the code enumsort.c
- gcc –pthread enumsort.c time.c –o enum

How may threads can we run concurrently?
What is the optimal number of threads to start?
What are the performance obstacles in the code?

Solution 1:
- Little work per task
- High overhead in creating and terminating threads
- More threads gives less synchronization points but more overhead in swapping threads in and out of cores

Solution 2:
Define larger tasks, let each task be to count the rank of \( \frac{\text{len}}{\text{nthreads}} \) elements => only one task per thread and totally \( \text{nthreads} \) tasks. Minimal synchronization and thread management overheads. (Study in lab 5)

Example: Numerical PDE Solver

\[ u_t + u_x + u_y = F(t, x, y) \quad 0 \leq x \leq 1, 0 \leq y \leq 1 \]
\[ \begin{cases}
  u(t, 0, y) = h_1(t, y) & 0 \leq y \leq 1 \\
  u(t, x, 0) = h_2(t, x) & 0 \leq x \leq 1 \\
  u(0, x, y) = g(x, y)
\end{cases} \quad \text{Initial Conditions} \]
\[ \text{Boundary Conditions} \]

Solve with explicit Finite Difference Method (\textit{Leapfrog}).
Core of the computations:

```plaintext
for k=2,Nt
    t=k*dt; Uold=U; U=Unew;
    for j=1,Ny-1
        for i=1,Nx-1
            x=i/Nx; y=j/Ny
            Unew(i,j)=Uold(i,j)+2*dt*(F(t,x,y)-
                (U(i+1,j)-U(i-1,j))/(2*dx)-
                (U(i,j+1)-U(i,j-1))/(2*dy))
        end for
    end for
end for
```

Where is the parallelism?
Update of each element (Unew(i,j)) is perfectly parallel within the k-loop.

Computational Stencil:

Divide grid over the threads, parallelize over j.
Parallel thread tasks: (leapfrog.c)

```c
for k=2,Nt
    thread_barrier();
    t=k*dt; Uold=U; U=Unew;
    for j=j1,j2
        for i=1,Nx-1
            x=i/Nx; y=j/Ny
            Unew(i,j)=Uold(i,j)+2*dt*(F(t,x,y)-
                (U(i+1,j)-U(i-1,j))/(2*dx)-
                (U(i,j+1)-U(i,j-1))/(2*dy))
        end for
    end for
end for
```

=> Perfectly parallel computations but need to synchronize in each time step (k-iteration).

**Note:** No need to have a barrier, just make sure that all threads are working with the same time step (iteration k). The inner points do not depend on other threads data, start computing on these points.
After computing on inner points check if all threads have reach the same time step, i.e., started to compute on its inner points.

```plaintext
for k=2,Nt
    thread_barrier_start(); // thread starts a new step
    t=k*dt; Uold=U; U=Unew;
    for j=j1+1,j2-1
        for i=1,Nx-1
            x=i/Nx; y=j/Ny
            Unew(i,j)=Uold(i,j)+2*dt*(F(t,x,y)-
                           (U(i+1,j)-U(i-1,j))/(2*dx)-
                           (U(i,j+1)-U(i,j-1))/(2*dy))
        end for
    end for
    thread_barrier_end(); // Wait until all threads have called the start-routine
    update Unew(:,j1) and Unew(:,j2)
end for
```

---

**Thread_barrier_start:**

```plaintext
pthread_mutex_lock(&lock);
ready++; locstep++;
if (ready==nthreads){
    ready=0;
    step++;
    pthread_cond_broadcast(&signal);
}
pthread_mutex_unlock(&lock);
```

**Thread_barrier_end:**

```plaintext
pthread_mutex_lock(&lock);
while (locstep>step)
    pthread_cond_wait(&signal,&lock);
pthread_mutex_unlock(&lock);
```
Performance 2x quad core processors:

- **Small grid:** Synchronization overhead becomes significant
Remark: Reduce thread swapping by letting master thread be peer in computations. This can have large impact when computational work (thread task) is small, avoid thread re-scheduling if the number of threads match the number of cores. Performance results also becomes less random without the extra thread.

```c
int main(int argc, char **argv){
    ...
    for (i=0; i<nthreads-1; i++)
        pthread_create(&thread[i],&attr,leapfrog,(void*)&arg[i]);
    leapfrog((void*)&arg[nthreads-1]);
    for (i=0; i<nthreads-1; i++)
        pthread_join(thread[i],NULL);

Example: Gram-Schmidt orthogonalization

for (i=0; i<n, i++) {
    /* Normalize Q[i] */
    norm=VecNorm(V[i]);
    for (k=0; k<n; k++) Q[i][k]=V[i][k]/norm;

    /* Orthogonal projection */
    for (j=i+1; j<n; j++){
        s=ScalarProd(Q[i],V[j]);
        for (k=0; k<n; k++)
            V[j][k]=V[j][k]-s*Q[i][k];
    }
}
```

Where is the parallelism?
The orthogonal projections of Q[i] on all V[j] for j=1 to n are perfectly parallel tasks.
Solution:

```c
for (i=0; i<n, i++){
    /* Normalize Q[i] */
    norm=VecNorm(V[i]);
    for (k=0; k<n; k++) Q[i][k]=V[i][k]/norm;

    /* Orthogonal projection */
    for(t=0; t<NUM_THREADS; t++){
        j1=i+1+(n-i-1)/NUM_THREADS*t;
        j2=i+1+(n-i-1)/NUM_THREADS*(t+1);
        pthread_create(&thread[t],&attr,proj,func_arg);
    }
    for(t=0; t<NUM_THREADS; t++)
        pthread_join(thread[t], &status);
}
```

```c
Proj:
for(j=j1;j<j2;j++){
    s= scalarProd(Q[i],V[j],n);
    for(k=0;k<n;k++) V[j][k] -=s*Q[i][k];
}
```

Task: Study, compile and run the program gram.c

- gcc –O3 –pthread gram.c time.c –o gram
- ./gram 1000   (run with 1000 vectors of length 1000)

How does the algorithm scale with the number of threads?
How does the algorithm scale if we change problem size?
(Run on different #threads, re do for different lengths.)

Is the scaling what you expected? If not, what are the performance obstacles in the code?
Performance results (Uppmax 2*intel i7, 8 cores):

<table>
<thead>
<tr>
<th>Number of threads</th>
<th>Time (1000)</th>
<th>Time (2000)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2.13</td>
<td>28.5</td>
</tr>
<tr>
<td>2</td>
<td>1.93</td>
<td>21.1</td>
</tr>
<tr>
<td>3</td>
<td>1.92</td>
<td>17.1</td>
</tr>
<tr>
<td>4</td>
<td>2.10</td>
<td>16.2</td>
</tr>
<tr>
<td>5</td>
<td>2.46</td>
<td>16.7</td>
</tr>
<tr>
<td>6</td>
<td>2.83</td>
<td>16.8</td>
</tr>
<tr>
<td>7</td>
<td>3.15</td>
<td>17.0</td>
</tr>
</tbody>
</table>

Parallel overheads:

- Frequent creation & termination of threads => synchronization in each iteration i.

- Serial section, normalization of Q[i] is not a part of the tasks (master computes).

- Data locality loss in projection between different iterations (j-iterations scheduled differently between different iterations).
\[ Q[0] = \frac{V[0]}{\text{norm}(V[0])} \]
\[ s = Q[0] \cdot V[1] \]
\[ V[1] = V[1] - s \cdot Q[0] \]
\[ s = Q[0] \cdot V[2] \]
\[ s = Q[0] \cdot V[3] \]
Etc all \( V[j] \)

\[ Q[1] = \frac{V[1]}{\text{norm}(V[1])} \]
\[ s = Q[1] \cdot V[2] \]
\[ s = Q[1] \cdot V[3] \]
Etc all \( V[j] \)

Solution 2:

```c
/* Create one lock per vector */
lock=(pthread_mutex_t *)malloc(n*sizeof(pthread_mutex_t));
for (i=0;i<n;i++) pthread_mutex_init(&lock[i], NULL);

/* Start parallel algorithm */
for (t=0; t<NUM_THREADS-1; t++)
    pthread_create(&thread[t], &attr, gram, (void *)t);

/* Master thread join computations */
t=NUM_THREADS-1;
gram((void *)t);

/* Synchronize threads, end parallel */
for (t=0; t<NUM_THREADS-1; t++)
    pthread_join(thread[t], &status);
```
Gram:

/* Compute 1:st Vector ahead */
if (thrid==0) Q[0]=V[0]/norm(V[0]);

/* Lock all vectors (unlock 1:st)*/
for (j=thrid;j<n;j+=NUM_THREADS) pthread_mutex_lock(&lock[j]);
if (thrid==0) pthread_mutex_unlock(&lock[0]);
Barrier();
for (i=1;i<n;i++){
/* Check if Q[i-1] is computed */
pthread_mutex_lock(&lock[i-1]);
pthread_mutex_unlock(&lock[i-1]);

/* Compute projection */
start=(i/NUM_THREADS)*NUM_THREADS; // or start=0
for (j=start+thrid;j<n;j+=NUM_THREADS)
  if (j>i-1) {
    s = scalarProd(Q[i-1],V[j]);
    V[j]=V[j]-s*Q[i-1];
    /* Compute Q[i] for next iteration */
    if (j==i) {
      Q[i]=V[i]/norm(V[i]);
      pthread_mutex_unlock(&lock[i]);
    }
  }
}

Performance results:

Note: The same technique can be used in other algorithms as well, e.g., LU-factorization.
=> Challenge (optional) task in lab 5
Summary:

Thread programming provides:

- **Software portability**, code runs unmodified on serial and parallel machines (shared memory).
- **Latency hiding**, can overlap threads waiting for memory, I/O, or communication with other tasks.
- **Scheduling and load balancing**, specify concurrent tasks dynamically and use system level mapping of tasks to cores. (Irregular load, e.g., games, web server)
- **Easy of programming**, compared to local name space models using message passing (MPI).
- **Effiency**, have detailed control of threads and data.

Summary:

To get good performance on Multi-core using Pthreads

- Find and assign large tasks for the threads
- Avoid frequent synchronization of threads
- Keep good cache locality on threads
- Keep good load balance between threads.
  Assign equal workload, also include master as peer.

- Other: Number of threads, thread attributes…?